

(\*  
Calculation implemented in Mathematica 6 by Frank Scheffold (Frank.Scheffold@unifr.ch),  
University of Fribourg (CH) and University of California Los Angeles (USA),  
January-March 2009 based on

"Measurable Structure Factor of a Multi-Species Polydisperse Percus-Yevick Fluid  
with Schultz distributed Paramters, M.Ginoza and M. Yasutomi, Journal  
of the Physical Society of Japan, 68, 1999, 2292-2297 - MONOCOMPONENT  
CALCULATION. Default values correspond to Figure 1c in the current JPCM  
article (particle size in micrometers, wavenumber q in inverse micrometers)  
\*)

$D\sigma := 0.044$ ;  $\eta := 0.77$ ;  $\sigma := 0.135$ ;  $\Delta := 1 - \eta$ ;  $t := \text{Abs}[1/D\sigma] - 1$ ;  $\text{poly} := 1/\sqrt{t+1}$ ;

(\*poly is the polydispersity index,  $\sigma$  is the mean particle diameter,  
 $\eta$  is the volume fraction of hard spheres\*)

poly

$t0 := 1$ ;  $t1 := 1$ ;  $t2 := \frac{(t+2)!}{t! * (t+1)^2}$ ;  $t3 := \frac{(t+3)!}{t! * (t+1)^3}$ ;

$\rho := \frac{6}{t3} * \frac{\eta}{\pi * \sigma^3}$ ;  $\xi0 := \rho$ ;  $\xi1 := \rho * \sigma$ ;  $\xi2 := \rho * \sigma^2$ ;  $\xi3 := \rho * \sigma^3$ ;  $F0 := \rho$ ;

$f0[x_] := t0 * \left(1 + \frac{x}{t+1}\right)^{-(t+1)}$ ;

$f1[x_] := t1 * \left(1 + \frac{x}{t+1}\right)^{-(t+1+1)}$ ;

$f2[x_] := t2 * \left(1 + \frac{x}{t+1}\right)^{-(t+2+1)}$ ;

$fa[x_] := \frac{1}{x^3} * \left(1 - \frac{x}{2} - f0[x] - \frac{x}{2} f1[x]\right)$ ;

$fb[x_] := \frac{1}{x^3} * \left(1 - \frac{x}{2} * t2 - f1[x] - \frac{x}{2} * f2[x]\right)$ ;

$fc[x_] := \frac{1}{x^2} * (1 - x - f0[x])$ ;

$fd[x_] := \frac{1}{x^2} * (1 - x * t2 - f1[x])$ ;

$F11[x_] := \frac{2 * \pi * \rho * \sigma^3}{\Delta} * fa[x]$ ;

$F21[x_] := \sigma * \frac{2 * \pi * \rho * \sigma^3}{\Delta} * fb[x]$ ;

$F12[x_] := \frac{1}{\sigma} * \left(\left(\frac{\pi}{\Delta}\right)^2 * \rho * \xi2 * \sigma^4 * fa[x] + \frac{\pi * \rho * \sigma^3}{\Delta} * fc[x]\right)$ ;

$F22[x_] := \left(\frac{\pi}{\Delta}\right)^2 * \rho * \xi2 * \sigma^4 * fb[x] + \frac{\pi * \rho * \sigma^3}{\Delta} * fd[x]$ ;

$FF11[s_] := 1 - F11[s * \sigma]$ ;

$FF12[s_] := -F12[s * \sigma]$ ;

$FF21[s_] := -F21[s * \sigma]$ ;

$FF22[s_] := 1 - F22[s * \sigma]$ ;

$G11[s_] := \frac{FF22[s]}{FF11[s] * FF22[s] - FF12[s] * FF21[s]}$ ;

$G12[s_] := \frac{-FF12[s]}{FF11[s] * FF22[s] - FF12[s] * FF21[s]}$ ;

$G21[s_] := \frac{-FF21[s]}{FF11[s] * FF22[s] - FF12[s] * FF21[s]}$ ;

$G22[s_] := \frac{FF11[s]}{FF11[s] * FF22[s] - FF12[s] * FF21[s]}$ ;

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I0[s_] := - $\frac{9}{2} \left( \frac{2}{s} \right)^6 * F0^2 \left( 1 - \frac{1}{2} (f0[-s*\sigma] + f0[s*\sigma]) + \right.$ 
 $\left. \frac{s*\sigma}{2} (f1[-s*\sigma] - f1[s*\sigma]) - \frac{s^2*\sigma^2}{8} (f2[-s*\sigma] + f2[s*\sigma] + 2*t2) \right);$ 
Ia1[s_] :=  $\frac{24}{s^3} F0 \left( -\frac{1}{2} (1 - f0[s*\sigma]) + \frac{s*\sigma}{4} (1 + f1[s*\sigma]) \right);$ 
Ia2[s_] :=  $\frac{24}{s^3} F0 \left( -\frac{\sigma}{2} (1 - f1[s*\sigma]) + \frac{s*\sigma^2}{4} (t2 + f2[s*\sigma]) \right);$ 
Iw1[s_] :=  $\frac{2*\pi*\rho}{\Delta*s^3} \left( Ia1[s] + \frac{s}{2} Ia2[s] \right);$ 
Iw2[s_] :=  $\frac{\pi*\rho}{\Delta*s^2} \left( 1 + \frac{\pi*\xi^2}{\Delta*s} \right) Ia1[s] + \frac{\pi^2*\xi^2*\rho}{2*\Delta^2*s^2} Ia2[s];$ 

h2[q_] :=
Iw1[ $\sqrt{-1} * q$ ] * G11[ $\sqrt{-1} * q$ ] *  $\frac{Ia1[\sqrt{-1} * q]}{I0[\sqrt{-1} * q]}$  + Iw1[ $\sqrt{-1} * q$ ] * G12[ $\sqrt{-1} * q$ ] *  $\frac{Ia2[\sqrt{-1} * q]}{I0[\sqrt{-1} * q]}$  +
Iw2[ $\sqrt{-1} * q$ ] * G21[ $\sqrt{-1} * q$ ] *  $\frac{Ia1[\sqrt{-1} * q]}{I0[\sqrt{-1} * q]}$  + Iw2[ $\sqrt{-1} * q$ ] * G22[ $\sqrt{-1} * q$ ] *  $\frac{Ia2[\sqrt{-1} * q]}{I0[\sqrt{-1} * q]}$ ;

SM[q_] := 1 - 2 * Re[h2[q]];

(*Monodisperse Percus Yevik - for comparison
a:= $\frac{(1+2*\eta)^2}{(1-\eta)^4}$ ; b:=- $\frac{3}{2} \frac{\eta(\eta+2)^2}{(1-\eta)^4}$ ;
f[u_] := 1 +  $\frac{24*\eta}{u^3} \left( a (\text{Sin}[u] - u*\text{Cos}[u]) + \right.$ 
 $\left. b \left( \left( \frac{2}{u^2} - 1 \right) u*\text{Cos}[u] + 2\text{Sin}[u] - \frac{2}{u} \right) + \frac{\eta*a}{2} * \left( \frac{24}{u^3} + 4 \left( 1 - \frac{6}{u^2} \right) \text{Sin}[u] - \left( 1 - \frac{12}{u^2} + \frac{24}{u^4} \right) u*\text{Cos}[u] \right) \right);$ 
SPY[q_] :=  $\frac{1}{f[q*\sigma]}$  *)

(*Data and Plots*)

(*us2=Table[{i,SPY[i]},{i,8,200,.2}];
ListPlot[{us2},PlotRange->{0,1.5}];*)

us = Table[{i, SM[i]}, {i, 8, 200, .2}];
ListPlot[{us}, PlotRange -> {0, 1.5}]

(*Export Data to File*)
(*Export["Documents/PY/temp",us3,"csv"]*)

0.209762

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